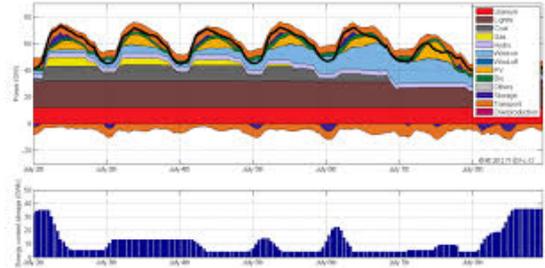


Title: optimization face to uncertainty on data

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Context: Data uncertainty is an inherent feature of optimization problems and has to be taken into account in optimization and decision-making tools. Uncertainty can come from noisy data (e.g. high-volatility financial markets), unreliable data (e.g. imprecise ratings in collaborative filtering), or uncertain predictions (e.g. different scenarios in forecasting). A typical example is the recent trend in electricity generation: the growing incorporation of renewable energy sources (wind, solar) in the electricity park has dramatically increased the level of uncertainty when optimizing electricity generation [1].



The three main paradigms in optimization under uncertainty and decision-making problems face to uncertainty consist in using

- approximations of the expected value of uncertain variables (i.e., stochastic optimization),
- a worst case value over an uncertainty set (i.e., robust optimization [2]),
- probability constraints of the form $\mathbb{P}(g(x, \xi) \geq 0) \leq \varepsilon$.

Though attractive in theory, the third one is much less developed because of two numerical drawbacks: 1) the probability constraints are not necessarily convex; 2) approximating the value of the probability function (and its gradients or Hessians when they exist [3]) involves noisy computations [5].

Objectives: This master thesis will consider theoretical and algorithmic questions in the above-described broad topic. Special interest will be given to design efficient algorithms to treat the nonconvex noisy probability-constrained optimization problems by extending bundle-type methods of nonsmooth optimization [4]. We will have important applications in electricity optimization, as a target. The aim would be to have contributions on three aspects: mathematical properties, algorithmic developments, and application on real-life data.

Practical information:

- Working place: LJK (Grenoble) or EDF research Department (Saclay), depending on the student.
- Salary: the master student will get the usual salary and gratifications.
- This project opens up to (academic or industrial) PhD thesis.

Keywords: nonsmooth optimization, convex analysis, bundle methods, energy applications

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