

**MASTER PROJECT PROPOSAL:**  
**Gas Diffusivity Inversion in Polar Firn Models**

Responsables :

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Keywords: Distributed systems, PDE modeling, inverse problems, climate change, atmospheric chemistry and physics.

**Framework:**

Polar ice cores provide a unique archive of atmospheric composition at time scales covering glacial-interglacial cycles (the last 800 000 years) to the rise of anthropogenic pollution (since about 1850 A.D.), as described in IPCC (2013), WMO (2014) and references therein. The measurements obtained in firn (upper part of the ice cap ~50-100 m, where air circulation occurs) provide information about the gas evolution during the anthropocene period (since about 1850 A.D.) while measurements from deeper ice allow us to look further in the past (e.g. natural and anthropogenic variations of methane sources over the last millennia and chaotic climate transitions since 60 000 years from isotopic ratios).

A 1-D inverse model, initially developed by Rommelaere et al., 1997, was recently extended to multi-gas (including isotopologues) and multi-sites analysis. The full procedure involves a suite of three models of gas transport in firn, generically referred to as the LGGE-GIPSA model (Witrant et al., 2012 and 2013). It provides a unique tool for reconstructing atmospheric scenarios and was used to interpret the data from several laboratories in the world.

**Expected results:**

The aim of this project is:

- 1) To study the uniqueness and stability of the 1-D inverse problem of recovering the diffusion coefficient of gases.
- 2) to improve the computation time of the diffusivity inversion part of the model by using alternative optimization methods/parameterized diffusivity models using data from multiple sites;

**Internship organization:** LJK (5 months) with regular visits/interactions with IGE and GIPSA.

**REFERENCES**

- H. Ammari, and F. Triki. Identification of an inclusion in multifrequency electric impedance tomography. Communications in Partial Differential Equations 42.1 (2017): 159-177.
- H. Ammari, F. Triki, and C-H. Tsou. Numerical determination of anomalies in multifrequency electrical impedance tomography. European Journal of Applied Mathematics 30.3 (2019): 481-504.
- E. Witrant, P. Martinerie, C. Hogan, J.C. Laube, K. Kawamura, E. Capron, S. A. Montzka, E.J. Dlugokencky, D. Etheridge, T. Blunier, and W.T. Sturges, "A new multi-gas constrained model of trace gas non-homogeneous transport in firn: evaluation and behavior at eleven polar sites", Atmos. Chem. Phys., 12, 11465-11483, 2012.
- E. Witrant and P. Martinerie, "A Variational Approach for Optimal Diffusivity Identification in Firns", Proc. of the 18th Mediterranean Conf. on Control and Automation, Marrakech, Morocco, June 23-25, pp 892-897, 2010.
- E. Witrant and P. Martinerie, "Input Estimation from Sparse Measurements in LPV Systems and Isotopic Ratios in Polar Firns", Proc. of the 5th IFAC Symp. on System Structure and Control, Grenoble, France, Feb. 4-6, 2013.